Online, December 2nd, 2023

parentheses • EN

Matter of Parentheses (parentheses)

Antonio loves brackets (or parentheses). He calls a sequence of '(' and ')' characters a "valid bracket sequence" if either:

- It's an empty sequence, or
- For each open bracket we can find a closed bracket on its right such that the substring between these two brackets forms a valid bracket sequence, and such that after removing that substring the remaining brackets also form a valid bracket sequence.



Figure 1: Brackets. Why not?

For example (()) and ()() are both valid, while)(and ())(() are not.

Furthermore, he calls a string of parentheses "K-valid" if, after adding K open brackets to its left and K closed brackets to its right, it is valid (either because it was valid before, or because it became valid).

For example (and ())(() are both 1-valid, while (is 2-valid.

Antonio is curious to find for any given N and K how many bracket sequences there are with length 2N that are K-valid. Because the result may be very large, Antonio is only interested in its remainder after dividing it by $1\,000\,000\,007$.

Help Antonio by writing a program that quickly calculates this number for Q different queries.

Input

The first line contains one integer Q, the number of queries Antonio is interested in.

The next N lines contain each a pair of integers: N_i and K_i .

Output

You need to write Q lines containing each the result of the i-th query: for each query, print the number of strings of length $2N_i$ that are K_i -valid, modulo $1\,000\,000\,007$.

Constraints

- $1 \le Q \le 100\,000$.
- $1 \le N_i \le 1000000$.
- $0 \le K_i \le 1000000$.

Examples

| input | output |
|-------|--------|
| 3 | 5 |
| 2 1 | 62 |
| 4 2 | 242 |
| 5 3 | |

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Explanation

In the first query there are 5 strings of length 4 that are 1-valid. They are highlighted below:

- In ((())) the sequence (()) is valid, but also 1-valid.
- In (()()) the sequence ()() is valid, but also 1-valid.
- In (())() the sequence ())(is invalid, but 1-valid.
- In ()(()) the sequence () (() is invalid, but 1-valid.
- In ()()() the sequence)()(is invalid, but 1-valid.

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